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2 *R. Thom.* Some “global” properties of differentiable manifolds

(Translated by V. O. Manturov with M. M. Postnikov’s comments (1958))

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